

Course Syllabus

Text: “Advanced Engineering Mathematics”, by Michael D. Greenberg, 2nd edition, Prentice Hall

The following is a list of the topics I intend to cover and the sections of the textbook that correspond to those:

Euler’s Formula: $e^{i\theta} = \cos \theta + i \sin \theta$

Fourier Series and PDEs

Chapter 17: Fourier Series

- 17.1 Introduction
- 17.2 Even, Odd, and Periodic Functions
- 17.3 Fourier Series of a Periodic Function
- 17.4 Half- and Quarter-range Expansions
- 17.5 Manipulation of Fourier Series
- 17.6 Vector Space Approach
- 17.7 The Sturm-Liouville Theory

Chapter 18: Diffusion Equation

- 18.1 Introduction
- 18.2 Preliminary Concepts
- 18.3 Separation of Variables

Chapter 17 and 18 (cont’d): Fourier Integral and Transforms

- 17.9 Fourier Integral
- 17.10 Fourier Transform
- 18.4 Fourier and Laplace Transforms

Chapter 19: Wave Equation

- 19.1 Introduction
- 19.2 Separation of Variables; Vibrating String
- 19.3 Separation of Variables; Vibrating Membrane
- 19.4 Vibrating String; d’Alambert’s Solution

Additional Topic: First Order Hyperbolic PDEs and the Method of Characteristics

Chapter 20: Laplace Equation

- 20.1 Introduction
- 20.2 Separation of Variables; Cartesian Coordinates
- 20.3 Separation of Variables; Polar Coordinates
- 20.4 Fourier Transform

Complex Variable Theory

Chapter 21: Functions of a Complex Variable

- 21.1 Introduction
- 21.2 Complex Numbers and the Complex Plane
- 21.3 Elementary Functions
- 21.4 Polar Form, Additional Elementary Functions, and Multi-valuedness
- 21.5 The Differential Calculus and Analyticity

Chapter 22: Conformal Mapping

- 22.1 Introduction
- 22.2 The Idea Behind Conformal Mapping
- 22.3 The Bilinear Transformation
- 22.4 Additional Mappings and Applications
- 22.5 More General Boundary Conditions
- 22.6 Applications to Fluid Mechanics

Chapter 23: Complex Integral Calculus

- 23.1 Introduction
- 23.2 Complex Integration
- 23.3 Cauchy's Theorem
- 23.4 Fundamental Theorem of the Complex Integral Calculus
- 23.5 Cauchy Integral Formula

Chapter 24: Taylor Series, Laurent Series, and the Residue Theorem

- 24.1 Introduction
- 24.2 Complex Series and Taylor Series
- 24.3 Laurent Series
- 24.4 Classification of Singularities
- 24.5 Residue Theorem