Problem of the Week

Proposed by Bernardo Ábrego and Silvia Fernández
October 30-November 6

Prove that the sequence

$$\left\{\left\lfloor \sqrt{2}\, n \right\rfloor\right\}, n = 1,2,3,\ldots$$

has an infinite number of powers of two.